

---

## The Role of GammaF ( $\gamma_f$ ) in Two-way Slab Punching Shear Calculations (CSA A23.3-14)

### Objective

Determine the adequacy of two-way (punching) shear strength around the exterior and interior columns in a typical two-way flat plate concrete floor system per CSA A23.3-14. Perform the unbalanced moment transfer calculations at slab-column connections. Determine the possible utilization of increased  $\gamma_f$  (GammaF) procedure in order to minimize or eliminate entirely the need for shear reinforcement.

### Codes

CSA A23.3-14, Design of Concrete Structures, Canadian Standards Association, 2014

### References

- [1] Notes on ACI 318-11 Building Code Requirements for Structural Concrete with Design Applications, Edited by Mahmoud E. Kamara and Lawrence C. Novak, Portland Cement Association, 2013
- [2] Wight J.K., Reinforced Concrete, Mechanics and Design, Seventh Edition, Pearson Education, Inc., 2016

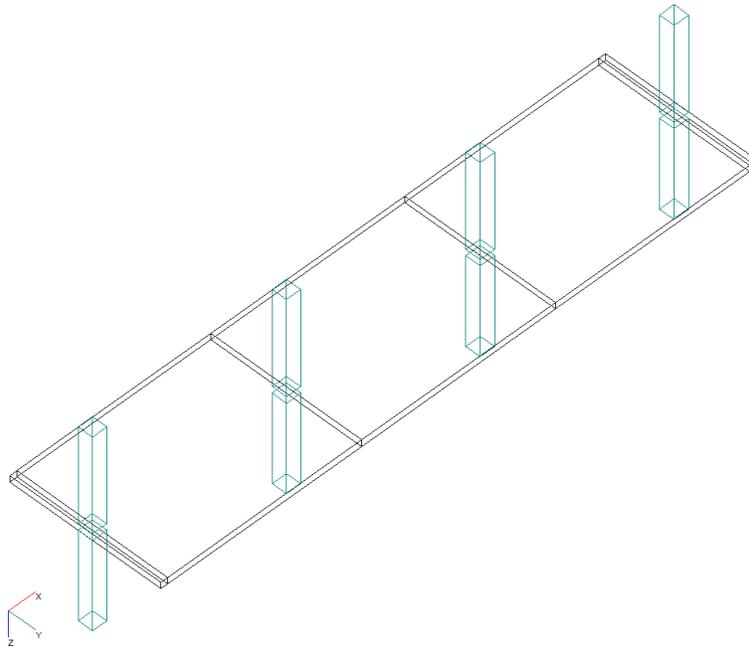
---

## Contents

Two-way Slab Model – Geometry & Design Data.....	3
Two-way (Punching) Shear Calculations .....	6
Computer Program Solution.....	14
Summary and Comparison of Results .....	16
Conclusions and Observations.....	16

## Two-way Slab Model – Geometry & Design Data

The isometric and plan views of the two-way flat plate concrete slab below are generated from an analytical model using the [spSlab](#) Program.



Slab thickness,  $h = 175$  mm

$d = 142$  mm

$f_c' = 25$  MPa (for slabs)

$f_c' = 35$  MPa (for columns)

$f_y = 400$  MPa

Isometric view of two-way flat plate concrete slab



### Exterior Columns

$c_1 = 400$  mm  $c_2 = 400$  mm

Location: Edge

Span direction: “Perpendicular to the edge”

Two-way shear perimeter dimensions

$b_1 = c_1 + d/2 = 400 + 142/2 = 471$  mm

$b_2 = c_2 + d = 400 + 142 = 542$  mm

$b_0 = 2 b_1 + b_2 = 1484$  mm

### Interior Columns

$c_1 = 400$  mm  $c_2 = 400$  mm

Location: Interior

Span direction: “Either direction”

Two-way shear perimeter dimensions

$b_1 = c_1 + d = 400 + 142 = 542$  mm

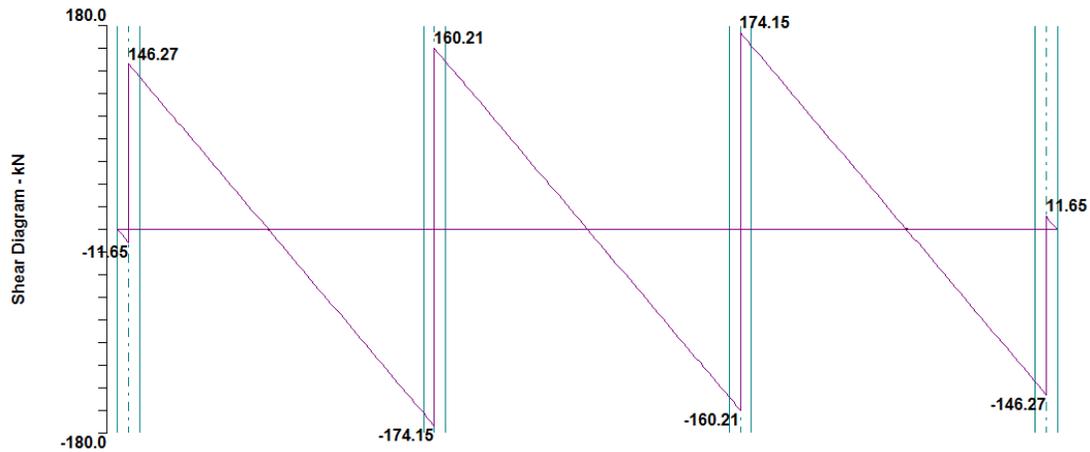
$b_2 = c_2 + d = 400 + 142 = 542$  mm

$b_0 = 2 b_1 + 2 b_2 = 2168$  mm

Plan view of two-way flat plate concrete slab

## Internal Force (Shear Force & Bending Moment) Diagrams

The shear force and bending moment diagrams below are produced by the [spSlab](#) Program.

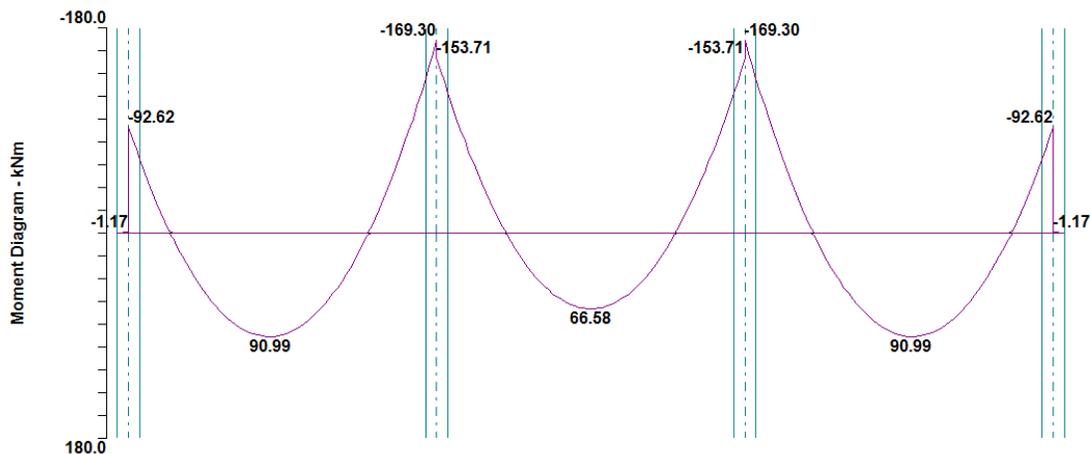


Shear Force Diagram from [spSlab](#)

From the shear force diagram, the factored shear force,  $V_{f,c}$ , that is resisted by the exterior and interior columns at a slab-column joint are:

At exterior supporting column:  $V_{f,c} = [146.27 + 11.65] = 157.92$  kN

At interior supporting column:  $V_{f,c} = [160.21 + 174.16] = 334.37$  kN



Bending Moment Diagram from [spSlab](#)

From the bending moment diagram, the factored slab moment,  $M_{f,c}$ , that is resisted by the exterior and interior columns at a slab-column joint are:

At exterior supporting column:  $M_{f,c} = [92.62 - 1.17] = 91.45$  kN-m

At interior supporting column:  $M_{f,c} = [169.30 - 153.71] = 15.59$  kN-m

CSA A23.3-14, clause 13.3.5.3 states that the fraction of factored slab moment resisted by the column,  $\gamma_v M_f$ , shall be assumed to be transferred by eccentricity of shear, where  $\gamma_v$  shall be calculated by:

$$\gamma_v = 1 - \frac{1}{1 + \left(\frac{2}{3}\right) \sqrt{\frac{b_1}{b_2}}}$$

where

$b_1$  = Dimension of the critical section  $b_o$  measured in the direction of the span for which moments are determined

$b_2$  = Dimension of the critical section  $b_o$  measured in the direction perpendicular to  $b_1$

CSA A23.3-14, 13.10.2 states that the fraction of factored slab moment resisted by the column,  $\gamma_f M_f$ , shall be assumed to be transferred by flexure, where  $\gamma_f$  shall be calculated by:

$$\gamma_f = 1 - \gamma_v$$

Compute the  $\gamma_f$  and  $\gamma_v$  values for exterior and interior column as follows:

$$\text{Exterior Column: } \gamma_v = 1 - \frac{1}{1 + \left(\frac{2}{3}\right) \sqrt{\frac{471}{542}}} = 0.383 \quad \text{and} \quad \gamma_f = 1 - 0.383 = 0.617$$

$$\text{Interior Column: } \gamma_v = 1 - \frac{1}{1 + \left(\frac{2}{3}\right) \sqrt{\frac{542}{542}}} = 0.400 \quad \text{and} \quad \gamma_f = 1 - 0.400 = 0.600$$

Per CSA A23.3-14, clause 13.10.2, all reinforcement resisting  $\gamma_f M_f$  shall be placed within the effective slab width,  $b_b$ , which is between lines that are one and one-half the slab thickness,  $1.5h$ , on each side of the column.

$$b_b = c_2 + 2 \times (1.5 \times h) = 400 + 2 \times (1.5 \times 175) = 925 \text{ in.}$$

Two-way slabs without beams that are modeled by spSlab need to have the effective slab width,  $b_b$ , located within the column strip width as defined by the Equivalent Frame Method (EFM). A detailed description of EFM is given in Chapter 2 of [spSlab Manual](#).

## Two-way (Punching) Shear Calculations

Two-way (punching) shear calculations are performed to ensure that the concrete slab design shear strength,  $v_r$ , shall be greater than or equal to the factored shear stress,  $v_f$ .

$$v_r \geq v_f$$

The combined two-way (punching) shear stress,  $v_f$ , is calculated as the summation of direct factored shear force alone and direct shear transfer resulting from the fraction of unbalanced factored moment:

$$v_f = \frac{V_f}{b_0} + \frac{\gamma_v M_f c_{AB}}{J_c}$$

where

$\gamma_v$  is the factor used to determine the fraction of unbalanced factored moment,  $M_f$  transferred by eccentricity of shear at the centroidal axis c-c of the critical section.

In accordance with the EFM solution, the transfer of moment from one principal direction at a time is to be considered and presented in this example. The transfer of moment from the orthogonal directions using consistent load cases and combinations needs to be accounted for separately. For a typical corner column, the orthogonal effects of the moment transfer would be quite significant.

The factored shear force,  $V_f = V_{f,c}$  for the interior and exterior columns

The factored self-weight and any factored superimposed surface dead and live load acting within the critical section can be subtracted from the factored reaction at the slab-column joint,  $V_{f,c}$ . This procedure is applied in spSlab Program and is more accurate. In this example, we will proceed with more conservative approach where

$$V_f = V_{f,c}$$

The factored unbalanced moment,  $M_f = M_{f,c} + V_{f,c} \times [c_1 / 2 - (c_{AB} - d / 2)]$  for the exterior column

The factored unbalanced moment,  $M_f = M_{f,c}$  for the interior column

The factored self-weight and any factored superimposed surface dead and live load acting within the critical section multiplied by moment arm,  $b_1 / 2 - (c_{AB} - d / 2)$  can be subtracted from the factored unbalanced moment,  $M_f$ .

For simplicity, spSlab Program utilizes  $c_1/2 - (c_{AB} - d/2)$  as the moment arm in  $M_f$  calculations. In this example, we will proceed with more conservative approach where  $M_f$  is calculated as shown above. Without shear reinforcement in the slab, the equivalent concrete stress corresponding to nominal two-way shear strength of slab,  $v_r$ , equals to the stress corresponding to nominal two-way shear strength provided by concrete,  $v_c$ .

$$v_r = v_c = \min \left[ 0.38\lambda\phi_c\sqrt{f'_c}, \left(1 + \frac{2}{\beta_c}\right)0.19\lambda\phi_c\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_0} + 0.19\right)\lambda\phi_c\sqrt{f'_c} \right]$$

$\phi_c$  = resistance factor for concrete

$\beta_c$  = the ratio of the long to the short side of the supporting column

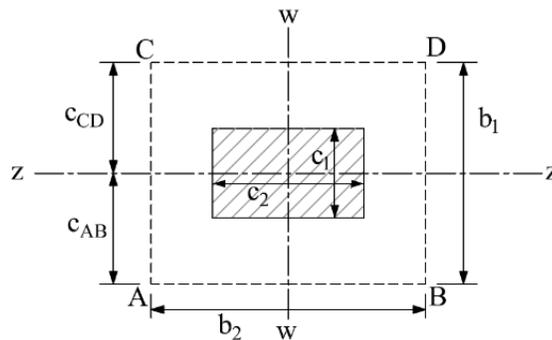
$\alpha_s$  = a constant dependent on supporting column location

$\lambda = 1.0$  (normal weight concrete)

$b_0$  = the perimeter of the critical section for two-way shear. The critical section shall be located so that the perimeter,  $b_0$ , is a minimum but need not be closer than  $d/2$  to the perimeter of the supporting column per CSA A23.3-14, clause 13.3.3.1.

**Interior column:**

Determine the section properties for shear stress computations.



Critical shear perimeter for interior column

**Critical Shear Perimeter for Interior Column**

The location of the centroidal axis z-z is:

$$c_{AB} = \frac{b_1}{2} = \frac{542}{2} = 271 \text{ mm}$$

The polar moment  $J_c$  of the shear perimeter is:

$$J_c = 2 \left( \frac{b_1 d^3}{12} + \frac{d b_1^3}{12} + (b_1 d) \left( \frac{b_1}{2} - c_{AB} \right)^2 \right) + 2 b_2 d c_{AB}^2$$

$$J_c = 2 \left( \frac{542 \times 142^3}{12} + \frac{142 \times 542^3}{12} + (542 \times 142)(0)^2 \right) + 2 \times 542 \times 142 \times 271^2 = 1.5331E + 10 \text{ mm}^4$$

The direct factored shear force,  $V_f = 334.37 \text{ kN}$

The factored unbalanced moment at the centroid of the critical section,  $M_f = 15.59 \text{ kN-m}$

The two-way shear stress ( $v_f$ ) can then be calculated as:

$$v_f = \frac{V_f}{b_0 \times d} + \frac{\gamma_v M_f c_{AB}}{J_c}$$

$$v_f = \frac{334.37 \times 1000}{2168 \times 142} + \frac{0.400 \times 15.59 \times 1000 \times 1000 \times 271}{1.5331E + 10}$$

$$v_f = 1.086 + 0.11 = 1.196 \text{ N/mm}^2$$

The two-way design shear strength without shear reinforcement,  $v_r$ , can be calculated as:

$$v_r = v_c = \min \left[ 0.38 \lambda \phi_c \sqrt{f'_c}, \left( 1 + \frac{2}{\beta_c} \right) 0.19 \lambda \phi_c \sqrt{f'_c}, \left( \frac{\alpha_s d}{b_0} + 0.19 \right) \lambda \phi_c \sqrt{f'_c} \right]$$

$$v_r = \min \left[ 0.38 \times 1 \times 0.65 \times \sqrt{25}, \left( 1 + \frac{2}{1} \right) \times 0.19 \times 1 \times 0.65 \times \sqrt{25}, \left( \frac{4 \times 142}{2168} + 0.19 \right) \times 1 \times 0.65 \times \sqrt{25} \right]$$

$$v_r = \min [1.235, 1.852, 1.469] \text{ N/mm}^2 = 1.235 \text{ N/mm}^2$$

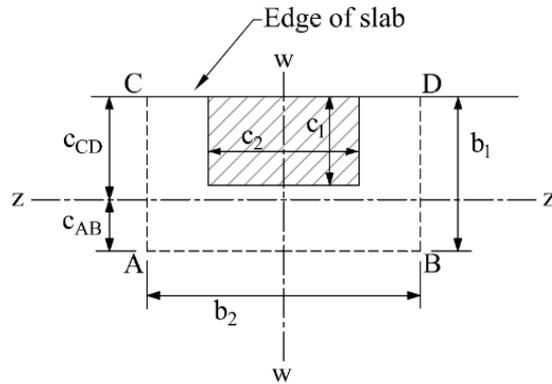
$$v_f / v_r = 1.196 / 1.235 = 0.97 < 1.00 \text{ O.K.}$$

Since  $v_r \geq v_f$  at the critical section, the slab has **adequate** two-way (punching) shear strength at the interior column.

Note that, it may be plausible to assume that the effect of moment transfer in the orthogonal direction would result in similar magnitude of the two-way shear stress as in this direction which is  $0.11 \text{ N/mm}^2$ .

**Exterior column:**

Determine the section properties for shear stress computations.



Critical shear perimeter for exterior column

**Critical Shear Perimeter for Exterior Column**

The location of the centroidal axis z-z is:

$$c_{AB} = \frac{\text{moment of area of the sides about AB}}{\text{area of the sides}} = \frac{2(471 \times 142 \times 471 / 2)}{2 \times 471 \times 142 + 542 \times 142} = 149.5 \text{ mm}$$

The polar moment  $J_c$  of the shear perimeter is:

$$J_c = 2 \left( \frac{b_1 d^3}{12} + \frac{d b_1^3}{12} + (b_1 d) \left( \frac{b_1}{2} - c_{AB} \right)^2 \right) + b_2 d c_{AB}^2$$

$$J_c = 2 \left( \frac{471 \times 142^3}{12} + \frac{142 \times 471^3}{12} + (471 \times 142) \left( \frac{471}{2} - 149.5 \right)^2 \right) + 542 \times 142 \times 149.5^2 = 5.4071E + 9 \text{ mm}^4$$

The direct factored shear force,  $V_f = 157.92 \text{ kN}$

The factored unbalanced moment at the centroid of the critical section,

$$M_f = 91.45 - 157.92 \times \left[ 200 - \left( 149.5 - \frac{142}{2} \right) \right] \times \left( \frac{1}{1000} \right) = 72.26 \text{ kN-m}$$

The two-way shear stress ( $v_f$ ) can then be calculated as:

$$v_f = \frac{V_f}{b_0 \times d} + \frac{\gamma_v M_f c_{AB}}{J_c}$$

$$v_f = \frac{157.92 \times 1000}{1484 \times 142} + \frac{0.383 \times (72.26 \times 1000 \times 1000) \times 149.5}{5.4071E+9}$$

$$v_f = 0.749 + 0.765 = 1.514 \text{ N/mm}^2$$

The two-way design shear strength without shear reinforcement,  $\phi v_n$ , can be calculated as:

$$v_r = v_c = \min \left[ 0.38 \lambda \phi_c \sqrt{f'_c}, \left( 1 + \frac{2}{\beta_c} \right) 0.19 \lambda \phi_c \sqrt{f'_c}, \left( \frac{\alpha_s d}{b_0} + 0.19 \right) \lambda \phi_c \sqrt{f'_c} \right]$$

$$v_r = \min \left[ 0.38 \times 1 \times 0.65 \times \sqrt{25}, \left( 1 + \frac{2}{1} \right) \times 0.19 \times 1 \times 0.65 \times \sqrt{25}, \left( \frac{3 \times 142}{1484} + 0.19 \right) \times 1 \times 0.65 \times \sqrt{25} \right]$$

$$v_r = \min [1.235, 1.852, 1.550] \text{ N/mm}^2 = 1.235 \text{ N/mm}^2$$

$$v_f / v_r = 1.514 / 1.235 = 1.23 < 1.00 \text{ N.G.}$$

Since  $v_r < v_f$  at the critical section, the slab has **inadequate** two-way shear strength at the exterior column.

Per CSA A23.3-14, the design needs to be modified. However, the two-way shear stresses at this exterior column can be reduced by modifying  $\gamma_f$  value per ACI 318-14, 8.4.2.3.4. The  $\gamma_f$  value may be increased up to 1.0, if the limitations on  $v_{ug}$  and  $\epsilon_t$  in ACI 318-14, Table 8.4.2.3.4 for edge column where span direction is perpendicular to the edge (i.e. exterior column in this example) are satisfied. The increase in the  $\gamma_f$  value effectively decreases the  $\gamma_v$  value which, in turn, helps reduce the two-way shear stresses in lieu of the other costly alternatives such as increasing the slab thickness, increasing column size, employing drop panels, employing column capitals, increasing the concrete strength,  $f'_c$ , or providing shear reinforcement.

This procedure as defined in ACI 318-14 is provided as an option in spSlab Program and may be utilized in order to arrive at a satisfactory design.

For this exterior column, ACI 318-14, Table 8.4.2.3.4 permits the maximum modified value of  $\gamma_f$  be 1.0 if

$$v_{ug} \leq 0.75\phi v_c \quad [v_f \leq 0.75v_r \text{ per CSA A23.3-14}]$$

where

$v_{ug}$  = factored shear stress on the slab critical section for two-way action due to gravity loads without moment transfer.

and

$$\varepsilon_t \geq 0.004 \text{ within } b_{slab} \quad [b_b \text{ per CSA A23.3-14}]$$

where

$\varepsilon_t$  = net tensile strain in extreme layer of longitudinal tension reinforcement at nominal strength, excluding strains due to effective prestress, creep, shrinkage and temperature.

Determine  $v_f$  as follows:

$$v_f = \frac{V_f}{b_0 \times d} = \frac{157.92 \times 1000}{1484 \times 142} = 0.749 \text{ N/mm}^2 \leq 0.75v_r = 0.75 \times 1.235 = 0.926 \text{ N/mm}^2 \quad \text{O.K.}$$

Determine the value of  $\gamma_v$  that is adequate for two-way shear design of the exterior column and the corresponding  $\gamma_f$  value as follows.

$$\frac{V_f}{b_0 \times d} + \frac{\gamma_v M_f^c}{J_c} = v_r$$

$$\frac{157.92 \times 1000}{1484 \times 142} + \frac{\gamma_v \times (72.26 \times 1000 \times 1000) \times 149.5}{5.4071 \text{E} + 9} = 1.235$$

$$0.749 + 2.0\gamma_v = 1.235$$

$$\gamma_v = \frac{1.235 - 0.749}{2.0} = 0.243$$

$$\gamma_f = 1 - \gamma_v = 1 - 0.243 = 0.757$$

Therefore, if the  $\gamma_f$  value is modified to 0.757, the two-way shear stress at this exterior column would be equal to two-way shear strength. Depending on the comfort level of the designer,  $0.757 \leq \gamma_f \leq 1.0$  can be utilized for this column provided that the  $\varepsilon_t$  requirement within  $b_b$  is met. In principle, a  $\gamma_f$  value closer to the lower-bound number (i.e. 0.757) would ensure better ductility while ensuring adequate two-way shear design. A  $\gamma_f$  value of 0.85 would provide approximately 15% cushion (i.e.  $v_f \approx 85\%$  of  $v_r$ ) for two-way shear. In this example, the  $\gamma_f$  value of 1.0 will be utilized to compare with spSlab Program where an option to invoke the upper bound value of  $\gamma_f$  is provided.

$$\gamma_f M_f = 1.0 \times 91.45 \text{ kN-m and } b_b = 925 \text{ mm}$$

$$\text{Assume } jd = 0.95 \times d = 0.95 \times 142 = 134.9 \text{ mm}$$

$$A_s = \frac{\gamma_f M_f}{\phi_s f_y jd} = \frac{1.0 \times 91.45 \times 1,000 \times 1,000}{0.85 \times 400 \times 0.95 \times 142} = 1994 \text{ mm}^2$$

$$\text{Try 10 - No. 15 bars. } A_s = 2000 \text{ mm}^2$$

Compute the depth of equivalent rectangular stress block,  $a$ , for  $A_s = 2000 \text{ mm}^2$ ; then recompute the  $A_s$  value using the computed value of the  $a$ :

$$a = \frac{A_s \phi_s f_y}{\alpha_1 \phi_c f'_c b} = \frac{2000 \times 0.85 \times 400}{0.813 \times 0.65 \times 25 \times 925} = 55.6 \text{ mm}$$

$$c = \frac{a}{\beta_1} = \frac{55.6}{0.908} = 61.2 \text{ mm} < \frac{700}{700 + f_y} \times d = \frac{700}{700 + 400} \times 142 = 90.4 \text{ mm}$$

Therefore, the section is tension-controlled and capacity reduction factor,  $\phi_s = 0.85$

$$A_s = \frac{\gamma_f M_f}{\phi_s f_y (d - a/2)} = \frac{1.0 \times 91.45 \times 1,000 \times 1,000}{0.85 \times 400 \times (142 - 55.6/2)} = 1932 \text{ mm}^2 < A_{s,prov} = 2000 \text{ mm}^2 \quad \text{O.K.}$$

The  $\epsilon_t$  requirement needs to be checked before accepting this design.

Using a linear strain distribution,

$$\epsilon_t = \epsilon_s = \frac{d - c}{c} \times \epsilon_{cu} = \frac{142 - 61.2}{61.2} \times 0.0035 = 0.0046 > 0.004 \quad \text{O.K.}$$

Therefore, modification of the  $\gamma_f$  value is permitted per ACI 318-14, 8.4.2.3.4.

The two-way shear stress ( $v_f$ ) is:

$$v_f = \frac{V_f}{b_0 \times d} + \frac{\gamma_v M_f c_{AB}}{J_c}$$

$$v_f = \frac{157.92 \times 1000}{1484 \times 142} + \frac{0.0 \times (72.26 \times 1000 \times 1000) \times 149.5}{5.4071E+9}$$

$$v_f = 0.749 + 0.0 = 0.749 \text{ N/mm}^2 \leq v_f = 1.235 \text{ N/mm}^2 \quad \text{O.K.}$$

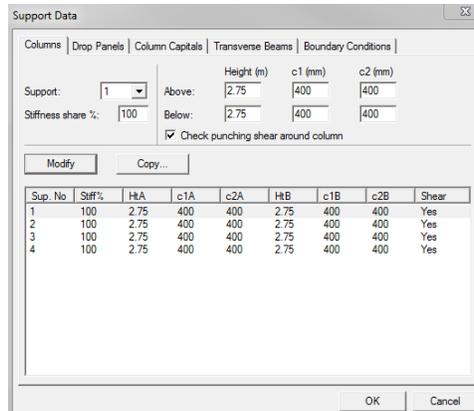
In flexural reinforcement calculations for unbalanced moment transfer by flexure, the utilization of an upper bound limit of 1.0 for  $\gamma_f$  results in 10 – No. 15 bars that need to be placed within  $b_b$  width of 925 mm. (i.e. upper limit of reliance of flexural reinforcement). On the other hand, in the two-way shear calculations, this results in a significant reserve capacity as the two-way shear stress is comprised of the direct shear only.

$$v_f / v_r = 0.749 / 1.235 = 0.61 \ll 1.00$$

This presents an opportunity to reevaluate the slab thickness and look for more economical option. Alternatively, a lower value of can be utilized to reduce additional flexural reinforcement and maximize the punching shear compared with the available allowable shear strength of the slab.

## Computer Program Solution

[spSlab](#) program provides an option to increase  $\gamma_f$  value per ACI 318-14 (to 1.0 in this exterior column case). However, since CSA A23.3-14 does not have a provision for this, the option is not available when utilizing CSA A23.3. The spSlab output below displays the solution without “increase  $\gamma_f$  option” where exterior column has inadequate two-way shear strength (CSA A23.3-14) and with “increase  $\gamma_f$  option” where exterior support has adequate punching shear strength:



Increase  $\gamma_f$  Option **NOT** available in CSA A23.3-14

Design Results - Band Reinforcement at Supports									
NOTE: <C> Total Strip, <B> Banded Strip, <S> Remaining Strip									
Support	Width <C>	Width <B>	Width <S>	As <C>	As <B>	As <S>	Bars <C>	Bars <B>	Bars <S>
	mm	mm	mm	mm <sup>2</sup>	mm <sup>2</sup>	mm <sup>2</sup>			
1	2150	925	1225	2200	1600	600	11-#15	8-#15	3-#15
2	2150	925	1225	2600	1200	1400	13-#15	6-#15	7-#15
3	2150	925	1225	2600	1200	1400	13-#15	6-#15	7-#15
4	2150	925	1225	2200	1600	600	11-#15	8-#15	3-#15

Design Results – Band Reinforcement at Supports from [spSlab](#)

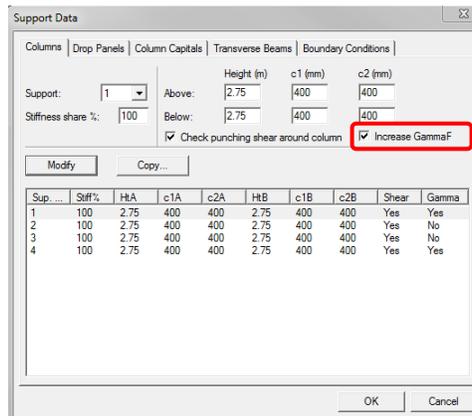
Design Results - Flexural Transfer of Negative Unbalanced Moment at Supports										
Support	Width	Width-c	d	Munb	Comb	Patt	$\gamma_f$	As,req	As,prov	Add Bars
	mm	mm	mm	kNm				mm <sup>2</sup>	mm <sup>2</sup>	
1	925	925	142	91.46	U2	All	0.617	1346	1600	---
2	925	925	142	15.59	U2	All	0.600	198	1200	---
3	925	925	142	15.59	U2	All	0.600	198	1200	---
4	925	925	142	91.46	U2	All	0.617	1346	1600	---

Design Results – Flexural Transfer of Negative Unbalanced Moment at Supports from [spSlab](#)

**Design Results - Punching Shear Around Columns - Punching Shear Results**

Support	Vu	vu	Munb	Comb	Patt	γv	vu	ΦVc	
	kN	N/mm <sup>2</sup>	kNm				N/mm <sup>2</sup>	N/mm <sup>2</sup>	
1	154.46	0.733	72.69	U2	All	0.383	1.503	1.235	*EXCEEDED
2	330.38	1.073	-15.59	U2	All	0.400	1.183	1.235	
3	330.38	1.073	15.59	U2	All	0.400	1.183	1.235	
4	154.46	0.733	-72.69	U2	All	0.383	1.503	1.235	*EXCEEDED

Design Results – Punching Shear Around Columns - Results *WITHOUT* Increase  $\gamma_f$  Option (CSA A23.3)



Increase  $\gamma_f$  Option (ACI 318) within spSlab

**Design Results - Flexural Transfer of Negative Unbalanced Moment at Supports**

NOTE: \*G - Increased GammaF factor.

Support	Width	Width-c	d	Munb	Comb	Patt	γf	As,req	As,prov	Add Bars
	mm	mm	mm	kNm				mm <sup>2</sup>	mm <sup>2</sup>	
1	925	925	142	91.46	U2	All	1.000	2107	602	8-#15 *G
2	925	925	142	15.59	U2	All	0.600	186	947	---
3	925	925	142	15.59	U2	All	0.600	186	947	---
4	925	925	142	91.46	U2	All	1.000	2107	602	8-#15 *G

Design Results – Flexural Transfer of Negative Unbalanced Moment at Supports from spSlab

**Design Results - Punching Shear Around Columns - Punching Shear Results**

NOTE: \*G - Decreased GammaV factor.

Support	Vu	vu	Munb	Comb	Patt	γv	vu	ΦVc	
	kN	N/mm <sup>2</sup>	kNm				N/mm <sup>2</sup>	N/mm <sup>2</sup>	
1	154.46	0.733	72.69	U2	All	0.000	0.733	1.246	*G
2	330.38	1.073	-15.59	U2	All	0.400	1.183	1.246	
3	330.38	1.073	15.59	U2	All	0.400	1.183	1.246	
4	154.46	0.733	-72.69	U2	All	0.000	0.733	1.246	*G

Design Results – Punching Shear Around Columns - Results *WITH* Increase  $\gamma_f$  Option (ACI 318-14)

## Summary and Comparison of Results

The comparison of the results of Hand and spSlab solutions for moment transfer between slab and column by flexure with modified  $\gamma_f$  values at the exterior column is tabulated below and the results are in good agreement.

Comparison of Reinforcement Required within the Effective Slab Width, $b_{slab}$ , for Moment Transfer between Slab and Column from Hand Solution and spSlab Solution		
Support Location	Exterior Column	
Solution Type	Hand	spSlab
Factored Slab Moment that is resisted by the Column at a joint, $M_f$ (kN-m)	91.46	91.46
The Factor used to determine the Fraction of $M_f$ Transferred by Slab Flexure at Slab-Column Connections, $\gamma_f$	1.0	1.0
The Fraction of $M_{sc}$ Transferred by Slab Flexure, $\gamma_f M_f$ , (kN-m)	91.46	91.46
Effective slab width, $b_b$ (mm)	925	925
$d$ (mm)	142	142

The modification of  $\gamma_f$  value as permitted by ACI 318 code enables a satisfactory design to replace costly alternatives such as thicker slabs, drop panels, column capitals, higher strength concrete, larger columns, or use of shear reinforcement.

## Conclusions and Observations

The modification of  $\gamma_f$  value as permitted by ACI 318 code enables a satisfactory design to replace costly alternatives to limit punching shear impact on concrete floor thickness.

- $\gamma_f$  is an important and useful tool that can be utilized to manage punching shear evaluation in lieu of costly options such as:
  - Increasing slab thickness
  - Increasing column size
  - Using drop panels
  - Using column capitals
  - Increasing slab  $f'_c$
  - Adding shear studs
- $\gamma_f$  offers the flexibility to transfer unbalanced moment by optimizing the proportion by which resistance is provided by the combination of shear and flexure.
- spSlab provides an upper-bound  $\gamma_f$  value for the user to evaluate punching shear options.